

A LETTERS JOURNAL EXPLORING THE FRONTIERS OF PHYSICS

### OFFPRINT

# Resistivity measurements unveil microscopic properties of CrAs

ANGELA NIGRO, PASQUALE MARRA, CARMINE AUTIERI, WEI WU, JINGUANG CHENG, JIANLIN LUO and CANIO NOCE

EPL, **125** (2019) 57002

Please visit the website
www.epljournal.org

Note that the author(s) has the following rights:

- immediately after publication, to use all or part of the article without revision or modification, **including the EPLA-formatted version**, for personal compilations and use only;

- no sooner than 12 months from the date of first publication, to include the accepted manuscript (all or part), **but not the EPLA-formatted version**, on institute repositories or third-party websites provided a link to the online EPL abstract or EPL homepage is included.

For complete copyright details see: https://authors.epletters.net/documents/copyright.pdf.

## AN INVITATION TO SUBMIT YOUR WORK

A Letters Journal Exploring

THE FRONTIERS OF PHYSICS

epljournal.org

### The Editorial Board invites you to submit your Letters to EPL

Choose EPL, and you'll be published alongside original, innovative Letters in all areas of physics. The broad scope of the journal means your work will be read by researchers in a variety of fields; from condensed matter, to statistical physics, plasma and fusion sciences, astrophysics, and more.

Not only that, but your work will be accessible immediately in over 3,300 institutions worldwide. And thanks to EPL's green open access policy you can make it available to everyone on your institutional repository after just 12 months.

#### Run by active scientists, for scientists

Your work will be read by a member of our active and international Editorial Board, led by Bart Van Tiggelen. Plus, any profits made by EPL go back into the societies that own it, meaning your work will support outreach, education, and innovation in physics worldwide.



epljournal.org

A LETTERS JOURNAL EXPLORING THE FRONTIERS OF PHYSICS







**21,500** citations in 2016

We greatly appreciate the efficient, professional and rapid processing of our paper by your team.

**Cong Lin** Shanghai University

#### Four good reasons to publish with EPL

International reach – more than 3,300 institutions have access to EPL globally, enabling your work to be read by your peers in more than 90 countries.



**Exceptional peer review** – your paper will be handled by one of the 60+ co-editors, who are experts in their fields. They oversee the entire peer-review process, from selection of the referees to making all final acceptance decisions.



**Fast publication** – you will receive a quick and efficient service; the median time from submission to acceptance is 75 days, with an additional 20 days from acceptance to online publication.



**Green and gold open access** – your Letter in EPL will be published on a green open access basis. If you are required to publish using gold open access, we also offer this service for a one-off author payment. The Article Processing Charge (APC) is currently €1,400.

Details on preparing, submitting and tracking the progress of your manuscript from submission to acceptance are available on the EPL submission website, **epletters.net**.

If you would like further information about our author service or EPL in general, please visit **epljournal.org** or e-mail us at **info@epljournal.org**.

#### EPL is published in partnership with:





Società Italiana di Fisica



sciences IOP Publishing

European Physical Society

EDP Sciences

IOP Publishing

epljournal.org



#### Resistivity measurements unveil microscopic properties of CrAs

ANGELA NIGRO<sup>1,2</sup>, PASQUALE MARRA<sup>3</sup>, CARMINE AUTIERI<sup>4</sup>, WEI WU<sup>5,6</sup>, JINGUANG CHENG<sup>5,6,7</sup>, JIANLIN LUO<sup>5,6,7</sup> and CANIO NOCE<sup>1,2</sup>

<sup>1</sup> Dipartimento di Fisica "E.R. Caianiello", Università degli Studi di Salerno - I-84084 Fisciano (SA), Italy

<sup>2</sup> CNR-SPIN, UOS di Salerno - I-84084 Fisciano (SA), Italy

<sup>3</sup> RIKEN Center for Emergent Matter Science - Wakoshi, Saitama 351-0198, Japan

<sup>4</sup> International Research Centre Magtop, Institute of Physics, Polish Academy of Sciences - Aleja Lotnikw 32/46, PL-02668 Warsaw, Poland

<sup>5</sup>Beijing National Laboratory for Condensed Matter Physics and Institute of Physics, Chinese Academy of Sciences Beijing 100190, China

<sup>6</sup>Songshan Lake Materials Laboratory, Dongguan - Guangdong 523808, China
 <sup>7</sup>School of Physical Sciences, University of Chinese Academy of Sciences - Beijing 100190, China

received 6 December 2018; accepted in final form 7 March 2019 published online 8 April 2019

PACS 72.10.Bg – General formulation of transport theory
 PACS 72.10.Di – Scattering by phonons, magnons, and other nonlocalized excitations
 PACS 74.70.-b – Superconducting materials other than cuprates

Abstract – We report resistivity measurements of a CrAs single crystal in a wide temperature range, with the specific aim to assess the applicability of the Bloch-Grüneisen formula for electron-phonon resistivity. We find that the resistance reaches a residual value at  $T_c \sim 4.2$  K and its temperature dependence cannot be fitted only with a suitable Bloch-Grüneisen formula in the whole temperature range, even though we are able to calculate a well-defined transport Debye temperature. The observed temperature-dependent resistivity seems to suggest a non–phonon-mediated superconducting pairing, supporting a magnetic fluctuation mechanism as the likely glue for the superconducting coupling.

Copyright © EPLA, 2019

**Introduction.** – The recent discovery of superconductivity in chromium arsenide CrAs has attracted a lot interest [1] because this material has been synthesized looking for superconductivity on the verge of the antiferromagnetic order by means of the application of external pressure [2]. The superconducting transition temperature  $T_c$  shows a dome-shaped pressure dependence, with a maximum  $T_c \sim 2.17$  K at a critical pressure  $P_c = 10$  kbar [2,3].

The corresponding temperature-pressure T-P phase diagram is reminiscent of those constructed for many quantum critical systems [4–10] except that the magnetic transition at ambient pressure is strongly first order, although the first-order signature is significantly weakened at elevated pressures [2,3,11]. We point out that in many recently discovered materials the superconductivity emerges near a magnetic quantum critical point. In these cases a high-temperature ordered state linked to spin, charge or lattice degrees of freedom is suppressed by means of the application of suitable external tuning parameters, such as the charge doping, chemical substitutions or the external pressure, as for the CrAs. Furthermore, the critical temperature  $T_c$  continuously passes through a maximum value giving rise to the celebrated dome-shaped  $T_c$  vs. tuning parameter phase diagram. Interestingly, it has been realized that the proximity to a magnetic phase may lead to new forms of superconductivity with non-conventional order parameter [12]. The systems where these effects have been identified include a large class of materials such the heavy-fermion compounds [13], the organic superconductors [14], the cuprate [15] and the ruthenate superconductors [16], and the iron-based materials [17].

At ambient pressure and low temperatures, the resistivity of CrAs follows a  $T^2$  power law, supporting a Fermi-liquid behavior [18]. The Kadowaki-Woods ratio is found to be  $10^{-5} \mu\Omega$  cm mole<sup>2</sup> K<sup>2</sup> mJ<sup>-2</sup>, which fits well to the universal value of many heavy-fermion compounds [19]. Nevertheless, the exponent n of the low-temperature behavior of resistivity, in the range between

the superconducting critical temperature and T = 10 K, and at the critical pressure, shows that  $n \sim 1.4$  [3], signalling a deviation from the Fermi-liquid behavior [20].

The first-order magnetic transition at the critical temperature  $T_N$  is signalled by an abrupt change of the lattice constants even though a lowering of the crystal structure symmetry has not been reported [21]. We point out that the interplay between structural, magnetic, and electronic properties at  $T_N$  [22] is rather conventional in transition metal compounds so that it is also expected to be crucial in CrAs, where the external pressure is the effective tool that settles the ground-state properties [23–25].

Muon spin rotation measurements performed on powder samples have revealed the existence of a region of coexistence, in the intermediate pressure region, where the superconducting and the magnetic volume fractions are spatially phase separated and compete with each other [26]. The phase separation scenario between magnetism and superconductivity together with the observation that the superfluid density scales with the critical temperature as ~  $T_c^{3.2}$  indicate a conventional mechanism of pairing in CrAs [26]. This conclusion is further supported by recent transport measurements on Al-doped CrAs single crystals [27].

Moreover, a nuclear quadrupole resonance under pressure [28] shows that the internal field in the helimagnetic state decreases slowly when the pressure increases, keeping a large value close to  $P_c$ . This result suggests, as previously stated, that the pressure-induced suppression of the magnetic order is of the first order. It has also been found that the nuclear spin-lattice relaxation rate in CrAs shows substantial magnetic fluctuations, but does not display a coherence peak in the superconducting state, supporting an unconventional pairing mechanism [28]. Some direct measurements like NMR and neutron scattering indicate that there exist strong spin fluctuations in normal state of CrAs. Indeed, there is no coherence peak at  $T_c$  in NMR, and  $1/T_1$  shows  $T^3$  power law below  $T_c$  pointing towards line nodes in the gap function.

Very recently, it has been shown by means of neutron diffraction that coupled structural-helimagnetic order is suppressed at the pressure where the bulk superconductivity develops with the maximal transition temperature [29]. Moreover, this coupled order is also completely suppressed by phosphorus doping as in  $\operatorname{CrAs}_{1-x} \operatorname{P}_x$ , at a critical doping above which inelastic neutron scattering evidenced persistent antiferromagnetic correlations [29]. These issues provide a possible link between magnetism and superconductivity, thereby bringing out new insights into an unconventional superconductivity similarly to that occurring in the high- $T_c$  iron pnictides.

Summarizing, at present, no convincing picture emerges to support a conventional or an unconventional superconducting pairing in the CrAs.

In this letter, we report detailed resistivity measurements of single-crystal CrAs samples at an external pressure near to the critical one, and we investigate to what extent the normal state resistivity  $\rho_{tot}(T)$  behavior is consistent with the electron-phonon scattering mechanism. As we will show, the results give important insights into the microscopic properties of CrAs, suggesting that CrAs cannot be considered as a phonon-mediated superconductor pointing towards other mechanisms such as, for instance, a magnetic fluctuation one as the glue driving the superconductivity.

Sample preparation. – The CrAs crystals were grown using the Sn-flux method [18]. The starting materials were Cr (Cerac, powder, 99.9%), As (Alfa Aesar, powder, 99.99%), and Sn (Cerac, shot, 99.9%). All of the manipulations were done in an argon-filled glove box with moisture and oxygen levels less than 1 ppm. The materials with atomic ratio of Cr:As:Sn = 3:4:40 were added to an alumina crucible, which was placed in a quartz ampoule, and subsequently sealed under a reduced pressure of  $10^4$  Torr. The quartz ampoule was heated up to 650 °C for 10 h, held there for a period of 8 h, then heated up to 1000 °C for 15 h, held for 6 h, and slowly cooled down to 600 °C for 50 h. At this temperature, a liquid Sn flux was filtered by centrifugation. The resulting products were metallic needle-shaped black crystals with dimensions up to  $0.15 \times 0.15 \times 1 \,\mathrm{mm^3}$ . The crystals were grown along the *b*-axis and they are stable in air and water. An energy-dispersive X-ray (EDX) analysis on these crystals was carried out using a Hitachi S-2700 scanning electron microscope. The results show that the chemical compositions are 51(2)% Cr, and 49(2)% As. No Sn atoms were detected in the crystals analyzed. The resistivity was measured between 2 K and 300 K by the standard 4-probe method. The current was applied along the *b*-axis of the crystal. Hydrostatic high pressure was generated with a self-clamped piston-cylinder made of non-magnetic BeCu and NiCrAl alloys.

**Resistivity measurements: theory and experiments.** – The resistivity  $\rho_{tot}(T)$  of a metal can be expressed as the sum of two contributions:

$$\rho_{tot}(T) = \rho_0 + \rho(T), \tag{1}$$

where  $\rho_0$  is the temperature-independent finite term due to the presence of defects, impurities or grain boundaries, while  $\rho(T)$  accounts for the temperature-dependent electrical resistivity. When the electrons are scattered only by phonons, without the participation of reciprocal lattice vectors, as produced by Umklapp processes,  $\rho(T)$  is given by the Bloch-Grüneisen equation [30,31]. In the framework of this approach, the phonons that contribute to the electron-phonon interaction are the acoustic ones and the resistivity  $\rho(T)$  depends only by the Debye temperature  $\Theta_D$ , allowing us to estimate  $\Theta_D$  of the compound.

According to the Bloch assumptions, the temperaturedependent phonon contribution to the resistivity can be exactly derived. To this end, it is assumed that the pseudopotential form factor is constant and the lattice vibration spectra obey a Debye-like dispersion relation. Within this picture, the Umklapp processes are neglected so that the electrons couple only with longitudinal phonons. Approximating the Fermi surface and the first Brillouin zone to a sphere, one obtains the well-known Bloch-Grüneisen result. Thus, the temperature-dependent contribution to the resistivity in eq. (1) may be written as

$$\rho(T) = AT^p + \rho_{BG}(T). \tag{2}$$

Here, the first term accounts for the low-temperature behavior of the resistivity, while the second one is the Bloch-Grüneisen contribution. The explicit general form of  $\rho_{BG}(T)$  is obtained assuming that the so-called phonon transport coupling function  $\alpha_{tr}^2 F(\omega)$  may be approximated by  $\sim \omega^{n-1}$  [31]. This transport coupling function produces a generalized Bloch-Grüneisen resistivity

$$\rho_{BG}(T) = BI_{BG}^{(n)}(T), \qquad (3)$$

with

$$I_{BG}^{(n)}(T) = \frac{T^n}{C_n} \int_0^{\Theta_D/T} \mathrm{d}x \frac{x^n}{(e^x - 1)(1 - e^{-x})}.$$
 (4)

In eqs. (3), (4), B and  $C_n$  are two constants, while the only relevant parameter is the Debye temperature  $\Theta_D$ , allowing us to estimate  $\Theta_D$  of the compound. For completeness, we notice that if  $\alpha_{tr}^2 F(\omega) \propto \omega^4$ , one gets the well-known  $T^5$ power law [30].

At low temperatures, that is for  $T \ll \Theta_D$ , the resistivity as defined in eqs. (1), (2) can be modelled through a temperature power law which reads as

$$\rho_{tot}(T) = \rho_0 + AT^p + BT^n, \tag{5}$$

where the Bloch-Grüneisen term  $I_{BG}^{(n)}(T)$  approximates  $T^n$ , as derived from eq. (4).

Figure 1(a) shows the temperature dependence of the in plane electrical resistivity  $\rho_{tot}(T)$  for a selected CrAs single-crystal sample at ambient pressure and in zero magnetic field. We observe that  $\rho_{tot}(T)$  (red triangles) exhibits a typical metallic behavior over the reported temperature range. A drop in the electrical resistivity is observed at  $T_N = 270$  K indicating the presence of a magnetic transition. This magnetic transition occurs with a simultaneous structural distortion with the lattice parameter *b* increasing abruptly by 4%, while *a* and *c* decrease by less than 1%.

In the same figure 1(a) it is also reported  $\rho_{tot}(T)$  (black spheres) at the pressure P = 9.5 kbar, very close to the pressure at which the maximum  $T_c$  is attained [2]. First of all, we notice that a residual resistivity  $\rho_0$  equal to  $1.2 \,\mu\Omega$ cm is measured, and the large residual resistivity ratio,  $RRR = \rho(300 \,\text{K})/\rho_0 \simeq 300$ , confirms the high quality of the used CrAs single crystal. At this pressure, we observe no anomaly related to the magnetic transition, whereas a single-step superconducting transition is visible at  $T_c = 1.51 \,\text{K}$  with a transition width  $\Delta T_c = 0.12 \,\text{K}$ ,



Fig. 1: (a) Temperature dependence of the in-plane electrical resistivity  $\rho_{tot}$  for a CrAs single crystal in zero magnetic field and at ambient pressure (red triangles) and at applied pressure P = 9.5 kbar (black spheres). The inset reports the resistivity data at P = 9.5 kbar in the low-temperature region showing the superconducting transition at  $T_c = 1.51$  K. (b) The low-temperatures resistivity data below 35 K at P = 9.5 kbar. The red solid line is the best fit of eq. (5).

as shown in the inset of fig. 1(a). We point out that  $T_c$  has been evaluated as the temperature corresponding to 50% of the normal state resistivity at the onset of the superconducting transition  $\rho_n$ , while  $\Delta T_c$  is defined as the difference between the temperature corresponding to 90% and 10% of resistivity at the superconducting transition temperature drop.

Figure 1(b) shows the low-temperatures resistivity data below 35 K. The red solid line is the best fit of eq. (5). The data fitting yields p = 1, n = 3 and a residual resistivity  $\rho_0 = 1.1 \,\mu \,\Omega$ cm. Previous studies showed that the lowtemperature resistivity of many transition metal alloys [32] is well described by an exponent n = 3 rather than n = 5. In this case the electron scattering from s to d bands and/or electron-magnon scattering occurs giving rise to this temperature power law resistivity behaviour [33,34]. This result suggests that the phonon-mediated contribution is not able to reproduce the temperature trend of the resistivity.

In the temperature range [2; 250] K, a best fit of  $\rho_{tot}(T)$  as given by eqs. (1) and (2), with n = 3, with  $C_3 = 7.212$ ,



Fig. 2: The best fit (red solid line) of  $\rho_{tot}(T)$ , at P = 9.5 kbar, as given by eqs. (1) and (2) to the experimental data (black spheres), in the temperature range 2–250 K. The inset shows an enlarged view below 20 K.

and p = 1, to the experimental data has been carried out and shown in fig. 2 (red solid line). The Debye temperature  $\Theta_D$ , the coefficients A and B are considered as free fitting parameters: The best fit values we get are  $\Theta_D = (340 \pm 5) \text{ K}, B = (14.7 \pm 0.2)10^{-5} \,\mu\,\Omega\,\text{cm}\,\text{K}^{-3}$  and  $A = (0.13 \pm 0.01)\,\mu\,\Omega\,\text{cm}\,\text{K}^{-1}$ .

We point out that a deviation from the fitting model of the temperature behavior of resistivity is observed at high temperatures where the resistivity seems to saturate. In particular, a decrease in the slope  $d\rho/dT$  with increasing temperature is clearly recognized above  $\simeq 240$  K in fig. 2.

Final remarks. – We have shown that the temperature trend of  $\rho_{tot}(T)$  cannot be explained by the Bloch-Grüneisen contribution only since it is not enough to reproduce the experimental data, but we need an extra term accounting for non-phononic contributions. We point out that a similar temperature behaviour has been traced for BaVSe<sub>3</sub> and ascribed to electron-electron scattering. This mechanism dominates other scattering mechanisms, such as, for instance, the electron-phonon interaction, showing up a deviation from the n = 2 power law exponent of the temperature-dependent resistivity [35].

Moreover, it is well known that the resistivity measurements may give an estimation of the electron-phonon coupling strength relevant for superconductivity [36,37]. Thus, considering the fitting of the temperature behaviour of the resistivity, we may derive a rough estimation of the average electron phonon-coupling constant  $\lambda_{e-ph}$ . Picking up the measured value of the critical temperature  $T_c = 1.5$  K and the estimated Debye temperature  $\Theta_D =$ 340 K, through the BCS equation

$$T_c = 1.14\Theta_D \exp(-1/\lambda_{e-ph}),\tag{6}$$

we get  $\lambda_{e-ph} \sim 0.18$ . This value of  $\lambda_{e-ph}$  is very low so that it suggests a very weak coupling regime, hence supporting the hypothesis that the electron-phonon coupling plays a minor role in the formation of Cooper pairs [36,37].

Furthermore, in the framework of the Eliashberg theory [38], the Allen-Dynes formula [39] yields an estimate of the critical temperature, which accounts for the competition of the phonon-driven attractive interaction with the repulsive Coulomb interaction expressed by the parameter  $\mu^*$ . This parameter describes the Coulomb repulsion reduced by retardation and screening effects and is obtained using the formula given by Morel and Anderson for the retarded Coulomb potential [40]. For conventional superconductors, retardation effects are believed to be very important in view of the very different energy scales for the electrons and phonons. From the available data on the density of states of CrAs [41–44], we are able to estimate  $\mu^*$  [45], obtaining  $\mu^* = 0.12$ . Since this value is not very much reduced by retardation effects, and considering that an efficient screening is important in reducing this parameter sufficiently to allow for an electron-phonon driven superconductivity [46,47], we may conclude that CrAs differs from the conventional phonon picture, where retardation effects play a major role in reducing the electron-electron repulsion.

Therefore, even though no clear indication on the nature of the superconducting states is currently available, from our results we infer that the extremely low electronphonon coupling constant and the not strongly renormalized Coulomb screening parameter indicate that a non-phonon-mediated superconducting coupling is likely, hence supporting an electronic driven mechanism such as, for instance, a magnetic-mediating coupling.

\* \* \*

The work is supported by the Foundation for Polish Science through the IRA Programme co-financed by EU within SG OP.

#### REFERENCES

- [1] NORMAN M., Physics, 8 (2015) 24.
- [2] WU W., CHENG J., MATSUBAYASHI K., KONG P., LIN F., JIN C., WANG N., UWATOKO Y. and LUO J., *Nat. Commun.*, 5 (2014) 5508.
- [3] KOTEGAWA H., NAKAHARA S., TOU H. and SUGAWARA H., J. Phys. Soc. Jpn., 83 (2014) 093702.
- [4] SEO S., PARK E., BAUER E. D., RONNING F., KIM J. N., SHIM J.-H., THOMPSON J. D. and PARK T., Nat. Commun., 6 (2015) 7433.
- [5] VARMA C. M., Phys. Rev. Lett., 83 (1999) 3538.
- [6] NOCE C., BUSIELLO G. and CUOCO M., *Europhys. Lett.*, 51 (2000) 195.
- [7] NOCE C., VECCHIONE A., CUOCO M. and ROMANO A., Ruthenate and Rutheno-Cuprate Materials Unconventional Superconductivity, Magnetism and Quantum Phase Transitions (Springer Verlag, Berlin) 2002.
- [8] VAN DER MARELL D., MOLEGRAAF H. J. A., ZAANEN J., NUSSINOV Z., CARBONE F., DAMASCELLI A., EISAKI H., GREVEN M., KES P.H. and LI M., *Nature*, **425** (2003) 271.

- [9] JIANG S., XING H., XUAN G., WANG C., REN Z., FENG C., DAI J., XU Z. and CAO G., J. Phys.: Condens. Matter, 21 (2009) 382203.
- [10] SHIBAUCHI T., CARRINGTON A. and MATSUDA Y., Annu. Rev. Condens. Matter Phys., 5 (2014) 113.
- [11] NIU Q., YU W. C., YIP K. Y., LIM Z. L., KOTEGAWA H., MATSUOKA E., SUGAWARA H., TOU H., YANASE Y. and GOH S. K., *Nat. Commun.*, 8 (2017) 15358.
- [12] GOLL G., Unconventional Superconductors, Springer Tracts Mod. Phys., Vol. 214 (Springer, Berlin) 2006.
- [13] MOVSHOVICH R., JAIME M., THOMPSON J. D., PETRO-VIC C., FISK Z., PAGLIUSO P. G. and SARRAO J. L., *Phys. Rev. Lett.*, 86 (2001) 5152.
- [14] LEFEBVRE S., WZIETEK P., BROWN S., BOURBONNAIS C., JÉROME D., MÉZIÈRE C., FOURMIGUÉ M. and BATAIL P., *Phys. Rev. Lett.*, 85 (2000) 5420.
- [15] VAN HARLINGEN D. J., Rev. Mod. Phys., 67 (1995) 515.
- [16] MACKENZIE A. P. and MAENO Y., Rev. Mod. Phys., 75 (2003) 657.
- [17] MAZIN I. I., SINGH D. J., JOHANNES M. D. and DU M. H., *Phys. Rev. Lett.*, **101** (2008) 057003.
- [18] WU W., ZHANG X. D., YIN Z. H., ZHENG P., WANG N. L. and LUO J. L., *Sci. China*, **53** (2010) 1207.
- [19] KADOWAKI K. and WOODS S. B., Solid State Commun., 58 (1986) 507.
- [20] DEMUER A., JACCARD D., SHEIKIN I., RAYMOND S., SALCE B., THOMASSON J., BRAITHWAITE D. and FLOU-QUET J., J. Phys.: Condens. Matter, 13 (2001) 9335.
- [21] SHEN Y., WANG Q., HAO Y., PAN B., FENG Y., HUANG Q., HARRIGER L. W., LEAO J. B., ZHAO Y., CHISNELL R. M., LYNN J. W., CAO H., HU J. and ZHAO J., *Phys. Rev. B*, **93** (2016) 060503(R).
- [22] KELLER L., WHITE J. S., FRONTZEK M., BABKEVICH P., SUSNER M. A., SIMS Z. C., SEFAT A. S., RONNOW H. M. and RÜEGG CH., *Phys. Rev. B*, **91** (2015) 020409(R).
- [23] CUOCO M., FORTE F. and NOCE C., Phys. Rev. B, 73 (2006) 094428.
- [24] CUOCO M., FORTE F. and NOCE C., Phys. Rev. B, 74 (2006) 195124.
- [25] CUOCO M., FORTE F. and NOCE C., Phys. Rev. B, 82 (2010) 155104.
- [26] KHASANOV R., GUGUCHIA Z., EREMIN I., LUETKENS H., AMATO A., BISWAS P. K., RÜEGG C., SUSNER M. A., SEFAT A. S., ZHIGADLO N. D. and MORENZONI E., *Sci. Rep.*, 5 (2015) 13788.

- [27] PARK S., SHIN S., KIM S., THOMPSON J. D. and PARK T., arXiv:1804.03816 (2018).
- [28] KOTEGAWA H., NAKAHARA S., AKAMATSU R., TOU H., SUGAWARA H. and HARIMA H., Phys. Rev. Lett., 114 (2015) 117002.
- [29] MATSUDA M., LIN F. K., YU R., CHENG J.-G., WU W., SUN J. P., ZHANG J. H., SUN P. J., MATSUBAYASHI K., MIYAKE T., KATO T., YAN J.-Q., STONE M. B., SI Q., LUO J. L. and UWATOKO Y., *Phys. Rev. X*, 8 (2018) 031017.
- [30] ZIMAN J. M., Electrons and Phonons: The Theory of Transport Phenomena in Solids (Oxford University Press, Oxford) 1960.
- [31] GRIMVALL G., The Electron-phonon Interaction in Metals (North-Holland, Amsterdam) 1981.
- [32] JIANG H., BAO J., ZHAI H., TANG Z., SUN Y., LIU Y., WANG Z., BAI H., XU Z. and CAO G., *Phys. Rev. B*, 92 (2015) 205107.
- [33] WHITE G. K. and WOODS S. B., Philos. Trans. R. Soc. A, 251 (1959) 273.
- [34] MOTT N. F., Adv. Phys., 13 (1964) 325.
- [35] AKRAP A., STEVANOVIĆ V., HERAK M., MILJAK M., BARIŠIĆ N., BERGER H. and FORRÓ L., *Phys. Rev. B*, **78** (2008) 235111.
- [36] ALLEN P. B., Phys. Rev. B, 36 (1987) 2920.
- [37] ALLEN P. B., in *Handbook of Superconductivity*, edited by POOLE C. (Academic, New York) 1999, pp. 478–483.
- [38] ELIASHBERG G. M., Sov. Phys. JETP, 11 (1960) 696.
- [39] ALLEN P. B. and DYNES R. C., Phys. Rev. B, 12 (1975) 905.
- [40] MOREL P. and ANDERSON P. W., Phys. Rev., 125 (1962) 1263.
- [41] AUTIERI C. and NOCE C., Philos. Mag., 97 (2017) 3276.
- [42] AUTIERI C., CUONO G., FORTE F. and NOCE C., J. Phys.: Condens. Matter, 29 (2017) 224004.
- [43] AUTIERI C., CUONO G., FORTE F. and NOCE C., J. Phys.: Conf. Ser., 969 (2018) 012106.
- [44] CUONO G., AUTIERI C., GUARNACCIA G., AVELLA A., CUOCO M., FORTE F. and NOCE C., to be published in *Eur. Phys. J. ST* (2018).
- [45] NIXON L. W., PAPACONSTANTOPOULOS D. A. and MEHL M. J., Phys. Rev. B, 76 (2007) 134512.
- [46] KOCH E., GUNNARSSON O. and MARTIN R. M., Phys. Rev. Lett., 83 (1999) 620.
- [47] BAUER J., HAN J. E. and GUNNARSSON O., Phys. Rev. B, 87 (2013) 054507.