

Enhanced orbital fluctuations in Mg-doped MnV_2O_4 single crystals

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We investigated the magnetic and structural transitions of $\text{Mn}_{1-x}\text{Mg}_x\text{V}_2\text{O}_4$ ($x = 0, 0.05, 0.1, 0.15$) single crystals with a normal spinel structure. These crystals all exhibit a cubic-to-tetragonal structural transition at T_S caused by the orbital ordering of V^{3+} ions, which is followed by a ferrimagnetic ordering transition at T_M . We found that T_M is equal to T_S for $x \leq 0.1$, but the ferrimagnetic transition is shifted to lower temperature by Mg doping and T_S and T_M can be separated clearly for $x = 0.15$. Moreover, a certain degree of orbital fluctuations was brought about by the ferrimagnetic transition at T_M , but suppressed below T^* , leading to another transition from weak orbital fluctuations to further orbital ordering at T^* . The orbital fluctuations were caused by the anomalous interchain interaction J^c and can be also enhanced by the substitution of Mg for Mn due to the decrease of the distance between V^{3+} ions along the c direction ${}^cR_{v-v}$, which results in the increase of J^c .

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I. INTRODUCTION

Transition-metal vanadium oxides with normal spinel structure (AB_2O_4) have attracted considerable interest because of some intriguing physical phenomena, such as orbital ordering, geometrical frustration, and multiferroicity [1–4]. The V^{3+} ion in AV_2O_4 occupies the B site forming a geometrically frustrated pyrochlore lattice and can form orbital ordering at low temperature [5–10]. Accompanying the orbital ordering, AV_2O_4 usually undergoes a cubic-to-tetragonal structural transition, which partially releases the geometrical frustration and then leads to a long-range magnetic ordering [3,11,12]. Due to the intricate coupling among the orbital, spin, and lattice degrees of freedom, there are complex magnetic and structural transitions in some normal spinel AV_2O_4 ($A = \text{Mn, Fe, Co}$) [11–14].

MnV_2O_4 was usually reported to undergo two successive phase transitions at $T_S \sim 56$ K and $T^* \sim 52$ K, respectively [14–18]. In the early reports, it was believed that a magnetic ordering transition first occurs at T_S , and then a structural transition from the cubic to the tetragonal phase is induced by orbital ordering at T^* , accompanied with a collinear to noncollinear ferrimagnetic transition [15–17,19]. However, in recent years, some different viewpoints about the origin of these two transitions have been put forward. By using thermal expansion and variable temperature x-ray-diffraction (XRD) measurements, Suzuki *et al.* pointed out that the orbital ordering and structural transition first takes place at

T_S , accompanied with a non-collinear ferrimagnetic ordering [7], but they have found no extra transition at T^* . In addition, Myung-Whun *et al.* also argued that a structural transition and a ferrimagnetic ordering occur simultaneously at T_S based on the specific-heat and magnetic susceptibility measurements [14]. Nevertheless, many recent papers still supported that the ferrimagnetic ordering happens at a higher temperature than the structural transition temperature [20–23]. Thus, the nature of these two transitions of MnV_2O_4 remains under debate.

In addition, the pattern of orbital ordering in MnV_2O_4 is also highly controversial. Suzuki *et al.* proposed an A-type antiferro-orbital ordering via analyzing the XRD of MnV_2O_4 single crystal below T_S [7], but Chung *et al.* found that the ferro-orbital ordering should be more stable because the interchain exchange interaction is a strong antiferromagnetic interaction [24]. Garlea and Chung *et al.* also observed a spin-wave gap arising around T^* [17,25], indicating the existence of single-ion anisotropy. Such a magnetic anisotropy may be a consequence of the unquenched orbital moment of the V^{3+} ion, in support of an uncompleted orbital ordering in MnV_2O_4 . Therewith, Myung-Whun *et al.* further guessed the existence of orbital fluctuations below T^* in MnV_2O_4 [14]. These results indicate that the orbital state in MnV_2O_4 is very complex, and it is closely related to the transition at T^* . Due to the coupling between orbitals and lattice, the phonons would be scattered by fluctuating orbitals, which results in positive temperature dependence of phonon thermal conductivity [16,26,27]. By contrast, the phonon thermal conductivity would be enhanced with decreasing temperature after orbital ordering. Therefore, the thermal conductivity can be an effective tool to detect the orbital fluctuations indirectly.

In a Mott insulator like MnV_2O_4 , an orbital ordering determines sign of the superexchange interaction between spins.

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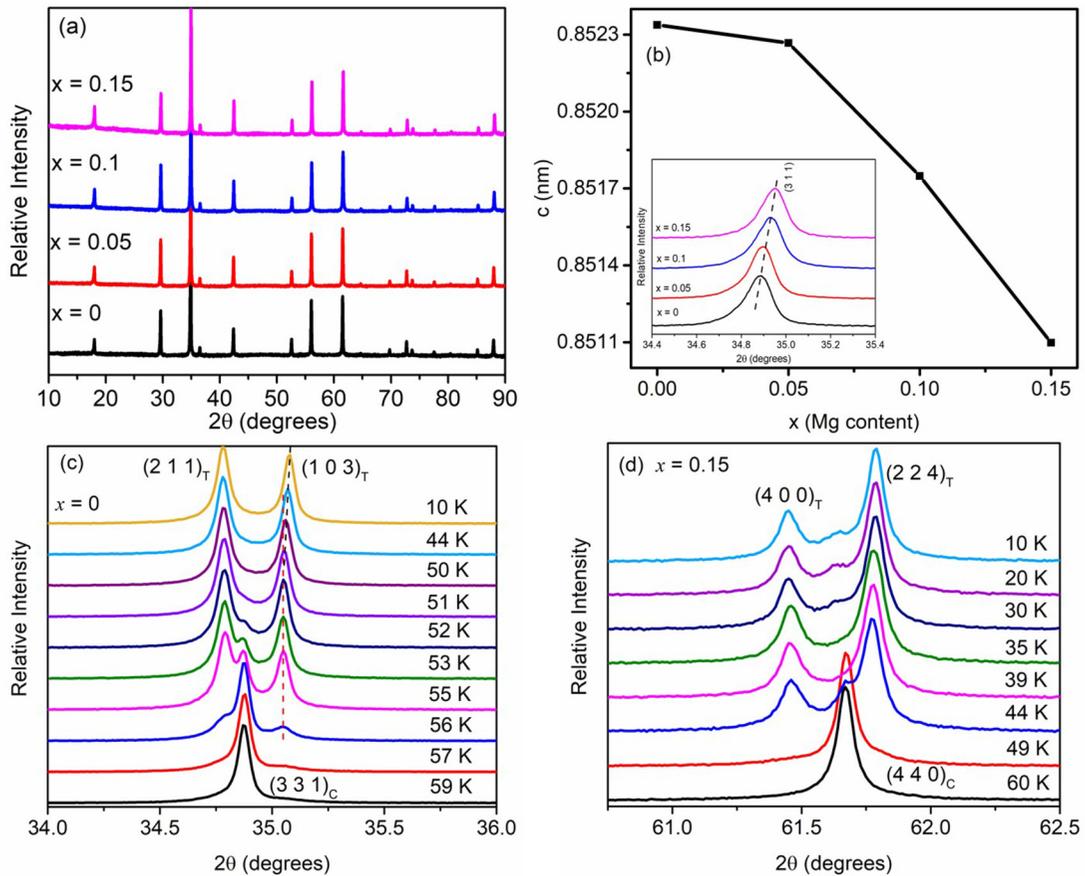


FIG. 1. (a), (b) The powder x-ray-diffraction patterns and lattice parameters for $\text{Mn}_{1-x}\text{Mg}_x\text{V}_2\text{O}_4$ ($x = 0, 0.05, 0.1, 0.15$) single crystals at room temperature. The inset in Fig. 1(b) displays the $(311)_C$ diffraction peaks of all samples. (c), (d) The variation temperature XRD patterns around the $(311)_C$ peak for $x = 0$ and around the $(440)_C$ peak for $x = 0.15$, respectively.

Since the distance between V^{3+} ions (R_{V-V}) can be changed by doping M^{2+} ion on the A site [28], the orbital ordering of MnV_2O_4 can be manipulated by the substitution of Mg for Mn. Therefore, we systematically studied the evolution of the magnetic and structural transitions in $\text{Mn}_{1-x}\text{Mg}_x\text{V}_2\text{O}_4$ ($x = 0, 0.05, 0.1, 0.15$) single crystals, which all exhibit a cubic-to-tetragonal structural transition at T_S , a ferrimagnetic ordering transition at T_M , and another transition at T^* . The structural transition at T_S is caused by the orbital ordering of V^{3+} ions, but a certain degree of orbital fluctuations arises below T_M due to the special magnetic interactions between V^{3+} ions, which can be suppressed at T^* . Moreover, with increasing Mg doping, the orbital fluctuations are enhanced gradually in $\text{Mn}_{1-x}\text{Mg}_x\text{V}_2\text{O}_4$, and the magnetic ordering transition temperature T_M was shifted to lower temperatures, which can be separated clearly from the structural transition at T_S for $x = 0.15$.

II. EXPERIMENT

Appropriate proportions of MnO , MgO , and V_2O_3 were mixed, ground together, and pressed into rods under 120-MPa hydrostatic pressure. Then the rods were calcined at 950 °C for 24 h in an evacuated sealed quartz tube. The single crystals of $\text{Mn}_{1-x}\text{Mg}_x\text{V}_2\text{O}_4$ ($x = 0, 0.05, 0.1, 0.15$) were grown by the optical floating-zone technique in pure argon atmosphere, and

the feed and seed rods rotate in opposite directions at 25 rpm during crystal growth at a rate of 14 mm/h. Small pieces of single crystal were ground into fine powder to check the phase purity and structural transition at low temperature by XRD. The temperature dependences of magnetic susceptibility $M(T)$ for $\text{Mn}_{1-x}\text{Mg}_x\text{V}_2\text{O}_4$ ($x = 0, 0.05, 0.1, 0.15$) crystals with unknown direction were measured under $H = 100$ Oe in zero-field-cooling (ZFC), field-cooled-cooling (FCC), and field-cooled warming (FCW) procedures, performed by the superconducting quantum interference device magnetometer. The measurements of specific heat $C_p(T)$ and thermal conductivity $\kappa(T)$ were performed by the physical property measurement system.

III. RESULTS AND DISCUSSION

As displayed in Figs. 1(a) and 1(b), the $\text{Mn}_{1-x}\text{Mg}_x\text{V}_2\text{O}_4$ ($x = 0, 0.05, 0.1, 0.15$) crystals all crystallize in the normal spinel structure with space group $Fd-3m$ at room temperature, and the lattice parameter a obtained from the Rietveld refinements shows a monotonic reduction with increasing Mg content because the ionic radius of Mg^{2+} ion (0.71 Å) is smaller than that of Mn^{2+} ion (0.80 Å). The low-temperature XRD patterns for $x = 0$ shown in Fig. 1(c) provide clear evidence for a cubic-to-tetragonal structural transition at $T_S = 56$ K due to the splitting of the $(311)_C$ peak into the $(103)_T$

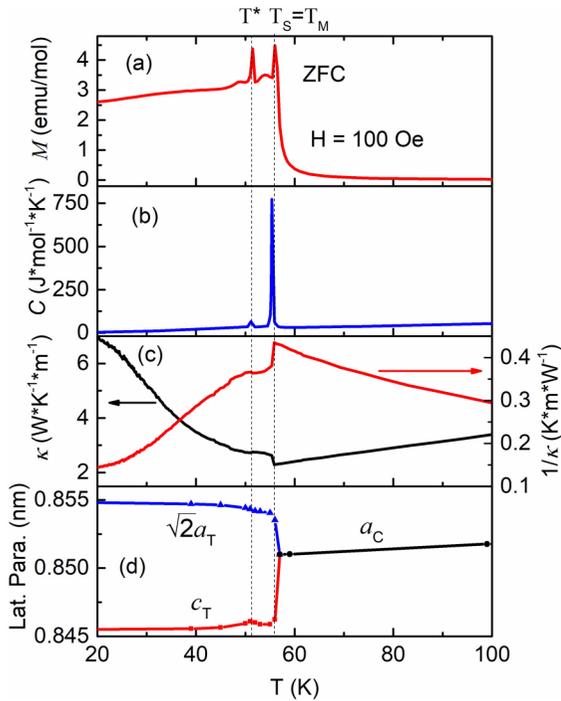


FIG. 2. (a)–(d) The temperature dependences of magnetic susceptibility, specific heat, thermal conductivity, and lattice parameter for MnV_2O_4 , respectively.

and $(211)_T$ peaks. Similar to that reported by Zhou *et al.* for pure MnV_2O_4 [16], these patterns also show the coexistence

of tetragonal and cubic phase in a narrow temperature range between 52 and 56 K. In addition, these crystals for $x = 0.05, 0.10$, and 0.15 also all exhibit a cubic-to-tetragonal structural transition, whose temperature lowers gradually with increasing x , as shown in Fig. 1(d) and Figs. 1(a) and 1(b) of Supplemental Material [29].

Figures 2(a)–2(d) show the temperature dependences of magnetic susceptibility $M(T)$, specific heat $C_p(T)$, thermal conductivity $\kappa(T)$, and lattice parameters for $x = 0$, respectively. All measurement data display two obvious transitions at the same temperatures ($T_S \sim 56$ K and $T^* \sim 51$ K). The transition at ~ 56 K has been confirmed to be a cubic-to-tetragonal structural transition by XRD patterns in Fig. 1(c), and the lattice parameter c_T in tetragonal phase shows a maximum value at $T^* \sim 51$ K, indicating an abnormal lattice distortion at T^* . Corresponding to that, the $(103)_T$ peak moves to the left above T^* and to the right below T^* with decreasing temperature, as shown in Fig. 1(c). The $M(T)$ increases rapidly at T_S , suggesting a ferrimagnetic ordering accompanied with the structure transition, which also causes a sharp specific-heat peak at T_S . The second magnetic transition occurs at T^* , where there is a distinct peak in $M(T)$ curve and a weak specific-heat peak. It is impossible to be a transition from collinear to noncollinear ferrimagnetism since the saturation magnetization above and below T^* are the same as shown in Fig. 2 of Supplemental Material [29]. Though its origin is still unclear, the simultaneous appearance of abnormal lattice distortion and magnetic transition suggests a strong spin-lattice coupling at T^* .

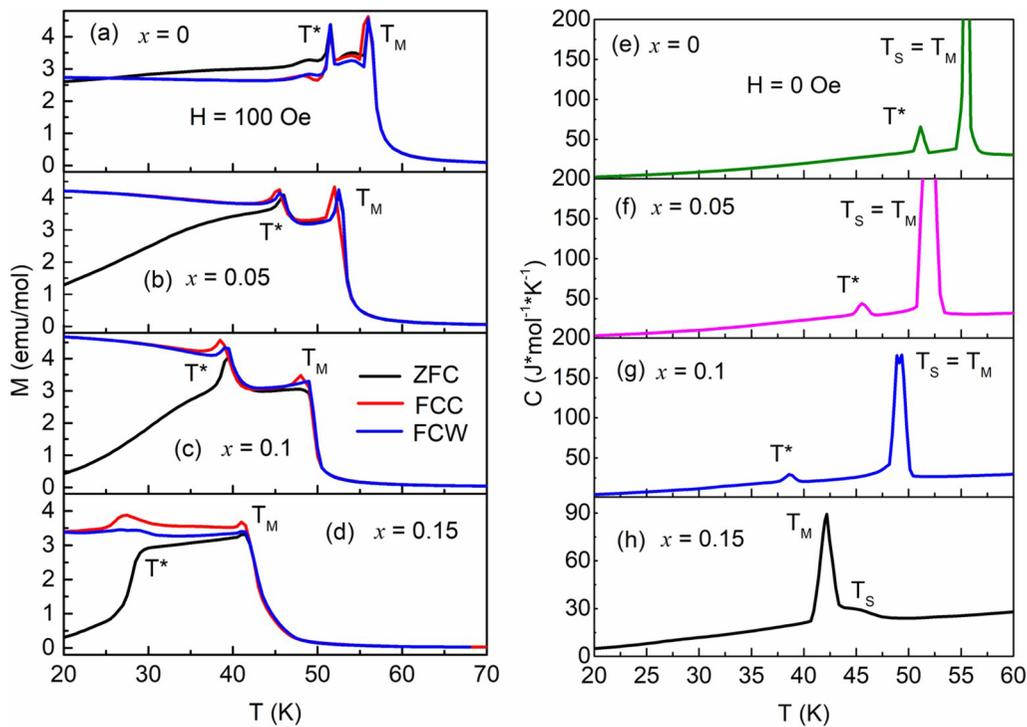


FIG. 3. (a)–(d) The temperature dependences of magnetic susceptibilities for $\text{Mn}_{1-x}\text{Mg}_x\text{V}_2\text{O}_4$ single crystals with unknown direction under $H = 100$ Oe in zero-field-cooling (ZFC), field-cooled-cooling (FCC), and field-cooled warming (FCW) procedures. (a) $x = 0$, (b) $x = 0.05$, (c) $x = 0.1$, (d) $x = 0.15$. (e)–(h) The specific heats for $\text{Mn}_{1-x}\text{Mg}_x\text{V}_2\text{O}_4$ single crystals under zero field. (e) $x = 0$, (f) $x = 0.05$, (g) $x = 0.1$, (h) $x = 0.15$.

As shown in Fig. 2(c), the negative temperature dependence of $1/\kappa$ above T_S reflects the strong scattering of phonons by disordered orbital [16]. At T_S , a steplike drop observed in the $\kappa(T)^{-1}$ curve indicates that an orbital ordering transition occurs at T_S . The $\kappa(T)^{-1}$ decreases slowly with lowering temperature between T_S and T^* , but the slope increases obviously below T^* , which maybe manifest that the phonon thermal conductivity is only partially restored at T_S and it is further recovered at T^* . Ishitsuka *et al.* reported that the thermal conductivities of AV_2O_4 ($A = \text{Mn, Fe, Co}$) are dominated by the fluctuations of the t_{2g} orbitals of V^{3+} [26,27]. The obvious slope change of $\kappa(T)^{-1}$ suggests that the transition at T^* maybe relate to the change of orbital state. Therefore, we can conclude that the cubic-to-tetragonal structure transition, ferrimagnetic ordering transition, and orbital ordering occur simultaneously at T_S for MnV_2O_4 , and the transition at T^* is associated with coupling among the orbital, spin, and lattice degrees of freedom.

For understanding the transition at T^* , we further analyzed the orbital ordering form in MnV_2O_4 . Suzuki *et al.* proposed that MnV_2O_4 has an A-type antiferro-orbital ordering, in which d_{yz} and d_{zx} orbitals form a chain along the $[110]$ and the $[\bar{1}\bar{1}0]$ directions, respectively, and both are alternately aligned along the c -axis [7]. According to the Goodenough-Kanamori rule, the A-type antiferro-orbital ordering would yield a strong intrachain antiferromagnetic interaction J^{ab} along the d_{yz} and d_{zx} orbital chains and a weak interchain ferromagnetic interaction J^c due to the inappreciable overlap between neighboring d_{yz} and d_{zx} . However, Chung *et al.* observed a large $J^c \sim 3.0$ meV by neutron scattering, meaning a strong antiferromagnetic interaction in MnV_2O_4 [21], which is inconsistent with the Goodenough-Kanamori rule. Moreover, except MnV_2O_4 , the J^c of other AV_2O_4 ($A = \text{Mg, Mn, Co, Fe, Zn}$) are all negative [2,11,30,31]. Thus, the anomalous J^c indicates that the A-type antiferro-orbital ordering may be unstable in MnV_2O_4 . Therefore, it is possible that a certain degree of orbital fluctuations may exist in MnV_2O_4 below the orbital ordering temperature T_S , and the orbital state of MnV_2O_4 can be further ordered below T^* , leading to the transition at T^* .

In order to verify our speculation about the transition at T^* , we further studied the $\text{Mn}_{1-x}\text{Mg}_x\text{V}_2\text{O}_4$ ($x = 0.05, 0.1, 0.15$) crystals, in which the J^c can be adjusted by the change of lattice parameter. The temperature dependences of magnetic susceptibility $M(T)$ and specific heat $C_p(T)$ for $\text{Mg}_x\text{Mn}_{1-x}\text{V}_2\text{O}_4$ ($x = 0, 0.05, 0.1, 0.15$) crystals are displayed in Figs. 3(a)–3(d) and 3(e)–3(h), respectively. All samples exhibit two significant magnetic transitions with clear thermal hysteresis at low temperature, marked as T_M and T^* , suggesting that they are first-order transitions. Except for $x = 0.15$, the $\text{Mn}_{1-x}\text{Mg}_x\text{V}_2\text{O}_4$ ($x = 0, 0.05, 0.1$) crystals all show two specific heat peaks at the same temperatures obtained in the $M(T)$ measurements. With increasing Mg concentration, the transition temperatures T_M and T^* are lowered progressively, and the magnitude of specific-heat peak at T^* is also suppressed gradually and completely disappears for $x = 0.15$. Moreover, besides the sharp peak at $T_M \sim 42$ K, there is still a shoulder at ~ 46.5 K in the $C_p(T)$ curve for $x = 0.15$. From Fig. 1(d), it can be seen that the $x = 0.15$ sample has a cubic phase at 49 K, but a tetragonal phase at

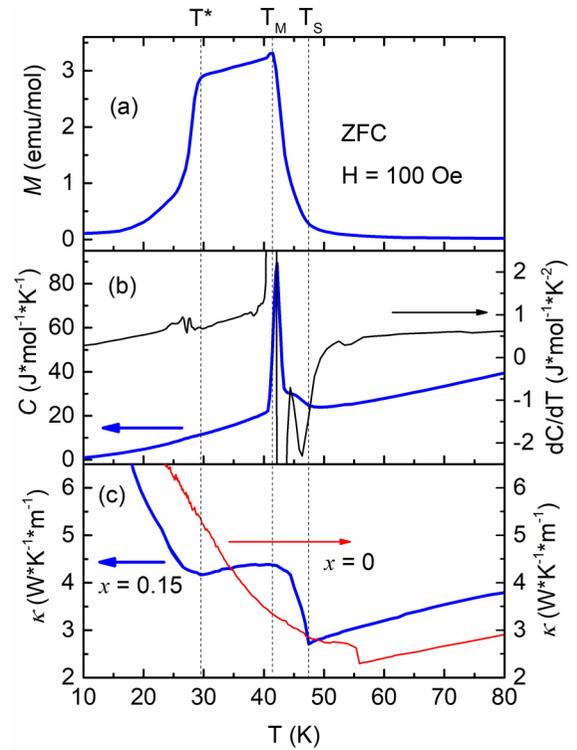


FIG. 4. (a) The variable-temperature magnetic susceptibility for $x = 0.15$. (b) The thick blue line is the specific heat $C_p(T)$ and the thin black line is the derivative of specific heat with respect to temperature $dC_p(T)/dT$. (c) The thermal conductivity for $x = 0.15$ (the thick blue line) and $x = 0$ (the thin red line).

44 K. Considering that the ferrimagnetic ordering occurs at ~ 42 K in $M(T)$ curve for $x = 0.15$, it can be concluded that the structural transition should take place at $T_S \sim 46.5$ K. These results indicate that the structure transition and ferrimagnetic transition are separated clearly by doping 15% Mg at Mn sites.

As shown in Fig. 4, besides the ferrimagnetic transition at T_M , the $dC_p(T)/dT$ for $x = 0.15$ also displays a sharp minimum at ~ 46.5 K, indicating a structure transition, and a small kink at ~ 27.5 K, which is approximately consistent with the T^* in $M(T)$ curve, though there is no obvious abnormality in the $C_p(T)$ curve. Moreover, the jumping temperature in $\kappa(T)$ is higher than the magnetic ordering temperature T_M in $M(T)$, but close to the transition temperature T_S obtained by lattice parameters and $dC_p(T)/dT$ curve, which proves again that the structure transition induced by orbital ordering occurs before the ferrimagnetic transition for $x = 0.15$. With decreasing temperature, the $\kappa(T)$ first increases slowly above T_M , but turns to decrease between T_M and T^* , showing the suppression of phonon thermal conductivity due to the existence of strong orbital fluctuations below T_M . With further decreasing temperature, the phonon thermal conductivity restores partially below T^* for $x = 0.15$, indicating again that the nature of the transition at T^* may be related to the transition from orbital fluctuations to orbital ordering. Though it can be seen from Figs. 1(c) and 1(d) that there is a small amount of cubic phase coexisting with main tetragonal phase below T_S , we still rule out the possibility that the orbital fluctuations are caused by the mixing of orbital disordered

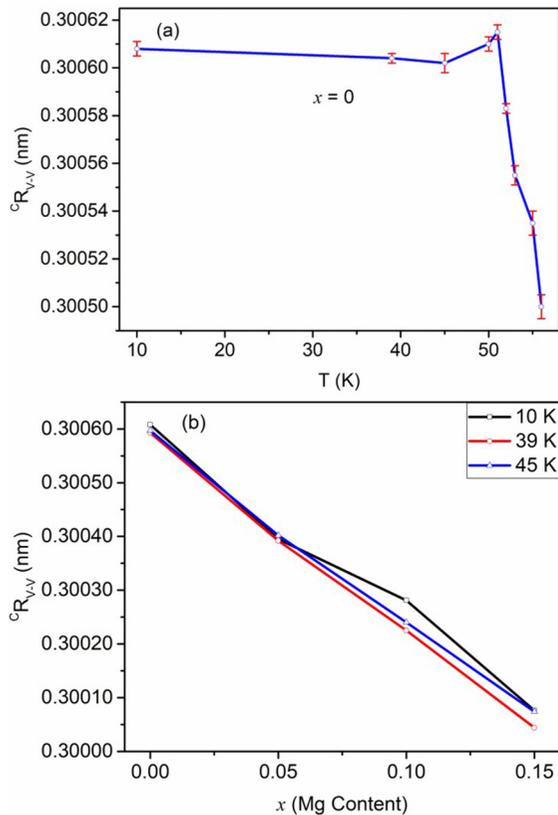


FIG. 5. (a) The temperature dependence of ${}^cR_{v-v}$ for $x = 0$. (b) The Mg content dependence of ${}^cR_{v-v}$ in tetragonal phase at 10, 39, and 45 K.

cubic phase based on the following two points. First, the orbital fluctuations still exist until $T^* \sim 29$ K, but the cubic phase disappears completely at ~ 39 K, which is much higher than T^* . Second, the orbital fluctuations for $x = 0.15$ occur below T_M instead of T_S . Therefore, it is reasonable to conclude that the orbital fluctuations are caused by magnetic ordering rather than structural transition, because the J^c can only be uniform after forming long-range magnetic ordering and then leading to the orbital fluctuations below T_M .

Because the orbital fluctuations are dominated by the anomalous large J^c , and the value of ${}^cR_{v-v}$ directly influences the overlap between neighboring d_{yz} and d_{zx} orbitals, the smaller ${}^cR_{v-v}$, the larger J^c , and the stronger orbital fluctuations. The variations of ${}^cR_{v-v}$ (the distance between V^{3+} ions along the c axis) obtained from the a and c lattice

parameters in the tetragonal phase are displayed in Fig. 5. The ${}^cR_{v-v}$ increases rapidly with decreasing temperature for $x = 0$ between T_S and T^* , suggesting that orbital fluctuations are suppressed gradually with lowering temperature above T^* and the further orbital ordering occurs at T^* . Furthermore, the ${}^cR_{v-v}$ in $Mn_{1-x}Mg_xV_2O_4$ solid solution at the same temperature decreases gradually with increasing Mg doping, as shown in Fig. 5(b). Thus, the J^c would gradually increase, leading to the enhancement of orbital fluctuations.

Considering that the Mg has a smaller atomic mass than Mn, replacing Mn by Mg would increase the thermal conductivity of MnV_2O_4 , just as shown above T_S . However, we note that the thermal conductivity for $x = 0.15$ is smaller than that for $x = 0$ below T^* . Though the $\kappa(T)$ increases upon decreasing temperature below T^* , the smaller value of $\kappa(T)$ indicates that phonon thermal conductivity is not completely restored for $x = 0.15$ below T^* , suggesting the presence of orbital fluctuations below T^* . Because the orbital fluctuations are enhanced gradually by doping Mg at Mn sites, the specific-heat peak at T^* , which originates from the reduction of orbital entropy, would monotonically weaken with increasing Mg content and disappears completely for $x = 0.15$.

IV. SUMMARY AND CONCLUSION

In conclusion, we have outlined the evolution of phase transitions in $Mn_{1-x}Mg_xV_2O_4$ ($x = 0, 0.05, 0.1, 0.15$) systems. All crystals show the cubic-to-tetragonal structure transition induced by orbital ordering at T_S , accompanied with the ferrimagnetic ordering transition. However, the abnormal large interchain interaction J^c disturbs the orbital ordering and causes a certain degree of orbital fluctuations below $T_M \sim T_S$. With decreasing temperature, the increasing ${}^cR_{v-v}$ reduces J^c , which suppresses the orbital fluctuations and further promotes the orbital ordering below T^* . The orbital fluctuations are enhanced by the substitution of Mg on Mn sites due to the increase of ${}^cR_{v-v}$. Simultaneously, the ferrimagnetic ordering temperature T_M is also reduced by Mg doping and can be separated clearly from structural transition temperature T_S for $x = 0.15$.

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